

PAPR Reduction Techniques with Hybrid SLM Partial Transmit Sequence Algorithm for OFDM System

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ABSTRACT

In recent time, the demand for multimedia data services has grown up rapidly. One of the most promising multi-carrier system, Orthogonal Frequency Division Multiplexing (OFDM) forms basis for all 4G wireless communication systems due to its large capacity to allow the number of subcarriers, high data rate and ubiquitous coverage with high mobility. OFDM is significantly affected by peak-to-average-power ratio (PAPR). In general; the high peak-to-average power ratio (PAPR) of transmitted signals for OFDM systems reduces the system efficiency and hence increases the cost of the radio frequency (RF) power amplifier. This thesis emphasis mainly on the PAPR reduction of OFDM system using partial transmits sequence (PTS) and pre-coding techniques. Some other techniques such as amplitude clipping have low-complexity; on the other hand, they suffer from various problems such as in-band distortion and out-of-band expansion. Signal companding methods have low-complexity, good distortion and spectral properties; however, they have limited PAPR reduction capabilities.

A modified hybrid algorithm is developed to obtain better PAPR reduction performance and reduce computational complexity compared with the conventional hybrid scheme. This proposed algorithm combines selected mapping (SLM) with partial transmit sequence (PTS) strategies, and further employs linear addition and exchange of various PTS sub-blocks to create more alternative OFDM signal sequences. As a result, with the same numbers of IFFT and phase rotation sequences, our proposed algorithm has the potentials to provide better PAPR reduction performance with lower computational complexity.

Keyword-- Orthogonal Frequency Division Multiplexing (OFDM), Peak-to-Average Power Ratio (PAPR), Partial Transmit Sequence (PTS), SLM

I. INTRODUCTION

The modern day phenomenon of increased thirst for more information and the explosive growth of new multimedia wireless applications have resulted in an increased demand for technologies that support very high speed transmission rates, mobility and efficiently utilize the available spectrum and network resources. Orthogonal Frequency Division Multiplexing (OFDM) is one of the best solutions to achieve this goal and it offers a promising choice for future high speed data rate systems [1]. The modulators and demodulators of OFDM systems can be simply implemented by employing inverse fast Fourier transform (IFFT) and FFT to make the overall system efficient and effective. Nowadays, it has been adopted as a powerfully potential candidate for next-generation mobile communications systems.

For OFDM-based systems, one of the main disadvantages is high PAPR problem. This phenomenon results from that in the time domain, an OFDM signal is the superposition of many narrowband subcarriers. At certain time instances, the peak amplitude of the signal is large and at the other times is small, that is, the peak power of the signal is substantially larger than the average power of the signal. The influence of high PAPR reduces system efficiency and then increases the cost of the RF power amplifier. Therefore, how to find a solution to reduce high PAPR effectively is one of the most important implementation issues in OFDM communications. The multiple signal representation is one of well-known PAPR reduction techniques for OFDM systems [2]. Several helpful schemes related to SLM-based and PTS-based techniques have been proposed for improving PAPR reduction performance or reducing the computational complexity. Those techniques included the conventional

hybrid method [3] and the modified SLM scheme [4]. Based on the preceding survey results, a novel modified hybrid algorithm combining the additional hybrid with switching hybrid schemes is proposed to reduce the number of IFFT and obtain a significant PAPR reduction performance in OFDM systems.

II. GENERATION OF OFDM SYMBOL

OFDM is simply defined as a form of multi-carrier modulation where the carrier spacing is carefully selected so that each sub carrier is orthogonal to the other sub carriers. Two signals are orthogonal if their dot product is zero. That is, if you take two signals multiply them together and if their integral over an interval is zero, then two signals are orthogonal in that interval. Orthogonality can be achieved by carefully selecting carrier spacing, such as letting the carrier spacing be equal to the reciprocal of the useful symbol period.

As the sub carriers are orthogonal, the spectrum of each carrier has a null at the center frequency of each of the other carriers in the system. This results in no interference between the carriers, allowing them to be spaced as close as theoretically possible. Mathematically, suppose we have a set of signals then

$$\begin{aligned} (t) &= k \text{ for } p=q \\ &= \text{for } p \neq q \end{aligned} \quad (1)$$

Where a_p and a_q are p th and q th elements in the set. The signals are orthogonal if the integral value is zero. Where, T is a symbol period. Since the carriers are orthogonal to each other the nulls of one carrier coincides with the peak of another sub carrier. As a result it is possible to extract the sub carrier of interest OFDM transmits a large number of narrowband sub channels. The frequency range between carriers is carefully chosen in order to make them orthogonal one another. In fact, the carriers are separated by an interval of $1/T$, where T represents the duration of an OFDM symbol.

A baseband OFDM symbol can be generated in the digital domain before, modulating on a carrier for transmission. To generate a baseband OFDM symbol, a serial digitized data stream is first modulated using common modulation schemes such as the phase shift keying (PSK) or quadrature amplitude modulation (QAM). These data symbols are then converted to parallel streams before modulating subcarriers. Subcarriers are sampled with sampling rate N/T , where N is the number of subcarriers and T is the OFDM symbol duration. The frequency separation between two adjacent subcarriers is $2/N$. Finally, samples on each subcarrier are summed together to form an OFDM sample. An OFDM symbol generated by an N -subcarrier OFDM system consists of N samples and the m th sample of an OFDM symbol is given by

$$x_m = \sum_{n=1}^N X_n e^{j \frac{2\pi mn}{N}} \quad 0 \leq m \leq N-1 \quad (2)$$

Where, X_n is the transmitted data symbol on the n th carrier. Equation (1.2) is equivalent to the N -point inverse discrete Fourier transform (IDFT) operation on the data sequence with the omission of a scaling factor. It is well known that IDFT can be implemented efficiently using inverse fast Fourier transform (IFFT). Therefore, in practice, the IFFT is performed on the data sequence at an OFDM transmitter for baseband modulation and the FFT is performed at an OFDM receiver for baseband demodulation. Size of FFT and IFFT is N , which is equal to the number of sub channels available for transmission, but all of the channels needs to be active. The sub-channel bandwidth is given by

Where, f_{sample} the sample rate and T_s is the symbol time. Finally, a baseband OFDM symbol is modulated by a carrier to become a band pass signal and transmitted to the receiver. In the frequency domain, this corresponds to translating all the subcarriers from baseband to the carrier frequency simultaneously.

III. PAPR REDUCTION TECHNIQUES

PAPR reduction methods can be mainly divided into two domain methods: frequency domain method and time domain method [14]. The basic notion of frequency domain method is to increase the cross correlation of the input signal before IDFT and decrease the output of the IDFT peak value or average value. Selective Mapping (SLM), Partial Transmit Sequence (PTS), Pre-coding etc. schemes are example of frequency domain method. However, in time domain method PAPR is reduced by distorting the signal before amplification and added of extra signals which increase the average power. Clipping and filtering, Peak widening etc. are examples of time domain method. It is very simple method because it requires very less computational time but introduces the distortion, increases out of band radiation and also degrades BER performance. On comparing between these two domain methods, frequency domain PAPR reduction technique is the most efficient one because of its ability to compress the PAPR without distorting the transmitted signal, no production of in band distortion and out of band radiation in OFDM signals.

Broadly PAPR reduction techniques are classified into four sections [15].

Signal scrambling (Probabilistic) technique

Signal Scrambling technique scramble each OFDM symbol with different scrambling techniques and select the sequence that gives the smallest PAPR value. It includes methods like Selective Mapping (SLM) and Partial Transmit Sequence (PTS).

Signal distortion technique

This technique reduces the PAPR by distorting the OFDM signal non-linearly. The methods like clipping and filtering, peak windowing, and non-linear companding are the example of this technique. These methods are applied after the generation of OFDM signal (after the IFFT).

Coding technique

The coding technique employed some error correcting codes for the PAPR reduction. These methods are applied before the generation of OFDM signal (before IFFT). When N signals are added with the same phase, they produce a peak power, which N is times the average power. The basic idea of all coding schemes for the reduction of PAPR is to reduce the occurrence probability of the same phase of many signals. The coding methods select such code words that minimize or reduce the PAPR. It causes no distortion and creates no out of band radiation, but it suffers from bandwidth efficiency as the code rate is reduced. It also suffered from the complexity to find the best codes and to store large lookup tables for encoding and decoding, especially for a large number of subcarriers. The error correcting codes like block codes, cyclic codes, Golay complementary sequence, Reed-Solomon (RS) code, Reed-Muller (RM) code, Hadamard code and Low Density Parity Check (LDPC) code can be used.

Pre-distortion technique

The pre-distortion technique is based on the reorientation or spreading the energy of data symbol before taking IFFT. The pre-distortion scheme includes DFT spreading, pulse shaping or pre-coding and constellation shaping.

IV. PROPOSED HYBRID SCHEMES

Conventional hybrid scheme

The conventional hybrid (CH) method combining the SLM with PTS schemes is investigated. The strategy was first explicitly proposed [6]; the block diagram of the CH method is shown in Figure 1. The original OFDM symbol is multiplied with the U phase rotation sequences, and then each of the new OFDM symbols is partitioned into V pairwise disjoint sub-blocks. Those OFDM sub-block values are calculated by each optimization of PTS blocks. For simplicity and without loss of generality, V = 2 is always considered in this paper. Each signal x(u), Where u = 1 . . . U, with the lowest PAPR is selected by each optimization block. They can be written as

$$(4)$$

$$(5)$$

Where, 1U

By the selection block, the relatively lower PAPR can be obtained from those lowest PAPR values of each PTS block. Because those lowest PAPR values of each PTS block are statistically independent to each other, the CCDF of CH scheme can be written as

$$= (6)$$

In order to recover transmitted data information, the receiver must have the knowledge of side information. Because the CH signal must include the side information of SLM and the side information of PTS, the number of required side information bits can be written as

$$(7)$$

Where W is the number of allowed phase rotation factors. In the first term expresses the SLM required side information bits and the second term is the additional bits from the PTS algorithm

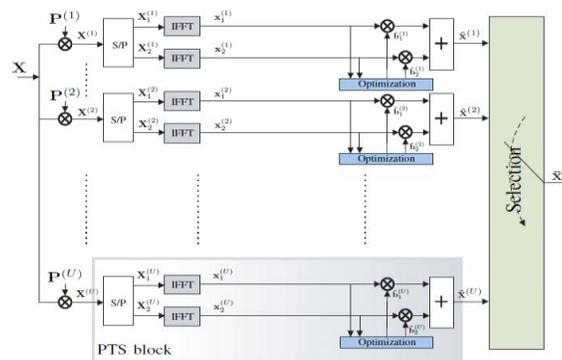


Figure 1: Block diagram of conventional hybrid scheme[16]

Additional Hybrid Scheme

In order to improve the PAPR reduction performance in CH scheme, we have to generate a large number of alternative OFDM signal sequences without increasing the number of IFFT to avoid high computational complexity. Here, a new additional hybrid (AH) scheme by combining the modified SLM scheme with CH scheme. The system performance is desirable that

the number of IFFT is reduced but the PAPR reduction performance is not compromised. The block diagram of AH scheme is shown in Figure 2.

Clearly, the first U signals x(u), where u = 1, . . . , U, are the same as the signals in the CH scheme. Furthermore, the alternative OFDM signal sequences are generated by the linear combination of the sub-block signals from different PTS blocks after IFFT operation.

Using the linear property of Fourier transform, the linear combination of these sequences can be obtained by

OFDM signal of lowest PAPR in AH scheme can be written as

$$(9)$$

$$(10)$$

Where, $U+1U^2$, We have to select and transmit the resulting OFDM signal sequence x , which has the

minimum PAPR among the whole OFDM signal sequences of overall lowest PAPR $x(u)$ sequences, which are composed by $\{ , \dots, \}$ after each optimization operation. The number of required side information bits for transmitter can be written as

$$(11)$$

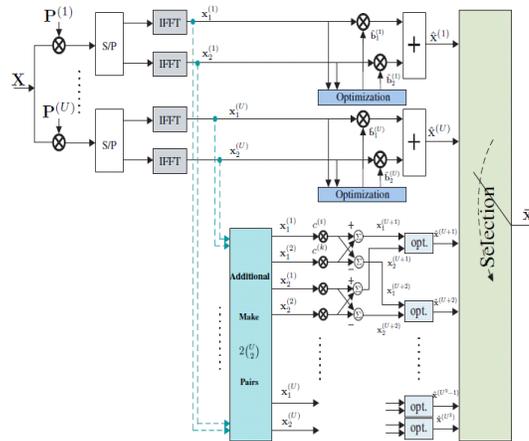


Figure 2: Block diagram of additional hybrid scheme[16]

Switching Hybrid Scheme

Instead of generating alternative OFDM sequences with linear combination, a new switching hybrid (SH) scheme by combining the switching technique with the CH scheme. The system performance is desirable that the number of IFFT is reduced but the PAPR reduction performance is not compromised. The block diagram of SH scheme is shown in Figure 3. By the switching block, we can use original U pairs to generate excessive 2 pairs of OFDM sequences without increasing the number of IFFT units. Thus, there are total U^2 pairs $\{ , \dots, \}$ are operated by each optimization unit. Obviously, the first U

signals, where $u = 1, \dots, U$, are the same as the signals in the CH scheme.

After the optimization blocks, the other alternative OFDM sequences with lowest PAPR can be written as

$$(12)$$

$$(13)$$

Where, $U+1U^2$, i, u and $In (4.10)$, and , come from different PTS blocks, which are generated by different phase rotation sequences, so that and , where i, u and can obtain differently alternative OFDM sequences with the minimum PAPR. Noteworthy, the number of required side information bits can be written as

$$(14)$$

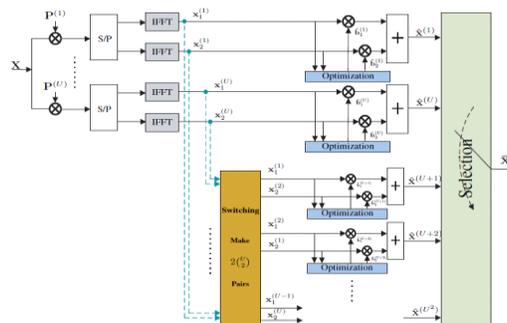


Figure 3: Block diagram of switching hybrid scheme[16]

Modified Hybrid Scheme

In order to further improve the PAPR reduction performance without increasing the number of IFFT, the modified hybrid (MH) algorithm is proposed by combining AH and SH schemes to generate more and more alternative OFDM sequences. Those $\{ \}$ pairs, where $1U$, are the signal inputs of the additional block and switching block respectively and simultaneously. The block diagram of MH scheme is shown in Figure 4.

Using the linear property of Fourier transform, the linear combination of U phase rotation sequences can obtain excessive 2 alternative OFDM sequences. After optimization blocks, those overall lowest PAPR can be written as the same as (10). Using the switching technique

among PTS blocks, the signals of U phase rotation sequences can obtain excessive 2 alternative OFDM sequences. After optimization blocks, those overall lowest PAPR can be written as the same as (13).

In the MH scheme, if $V = 2$ and U phase rotation sequences are considered, the original signals can generate excessive 2 pairs of sequences respectively and simultaneously by either additional block or switching block. Therefore, there are total OFDM sequences with the lowest PAPR in the MH scheme. In order to recover the transmitted data information, the number of required side information bits can be obtained by

$$(15)$$

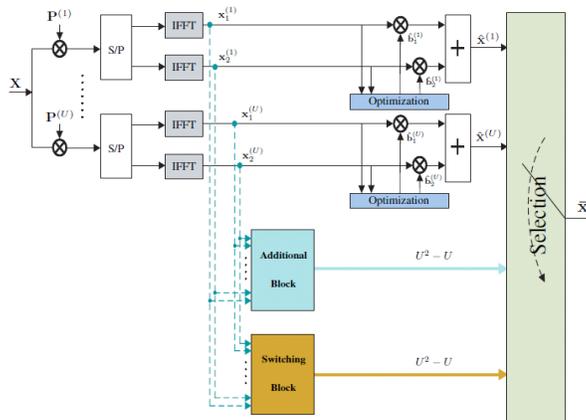


Figure 4: Block diagram of Modified hybrid scheme[16]

V. SIMULATION RESULTS

The PAPR reduction performance with the CH scheme for various values of U is shown in Figure 5. It

shows that the PAPR reduction performance becomes better as the number of U increases.

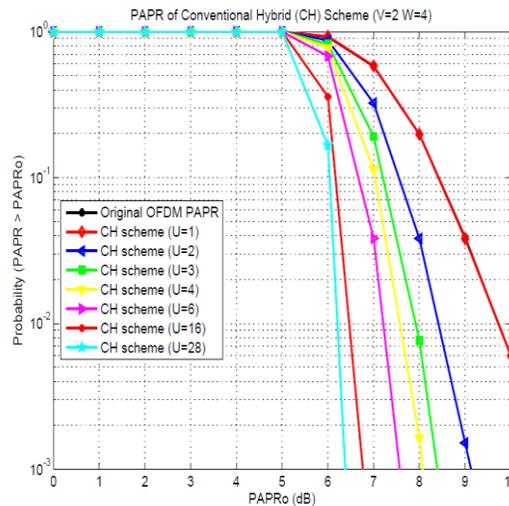


Figure 5: PAPR reduction performance of conventional hybrid scheme for OFDM systems

In Figure 5.2 and Figure 5.3, the performance of AH scheme is similar to that of SH scheme. The AH and SH schemes with $U = 2$ and $U = 4$ have almost the same performance compared with the CH scheme with $U = 4$

and $U = 16$, respectively. In Figure 5.4, the MH method with $U = 2$ and $U = 4$ has almost the same performance compared with the CH scheme with $U = 6$ and $U = 28$, respectively.

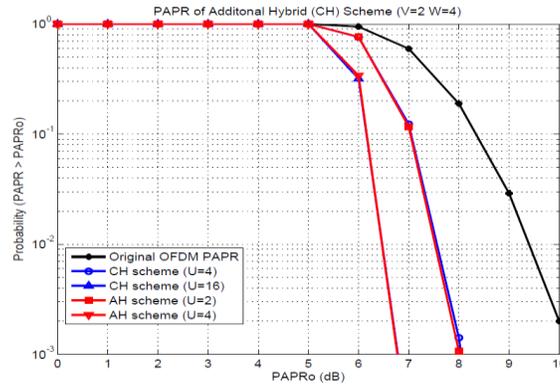


Figure 6: PAPR reduction performance of additional hybrid scheme for OFDM systems

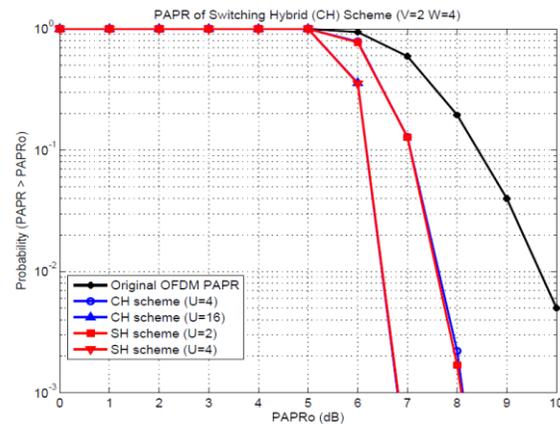


Figure 7: PAPR reduction performance of switching hybrid scheme for OFDM systems

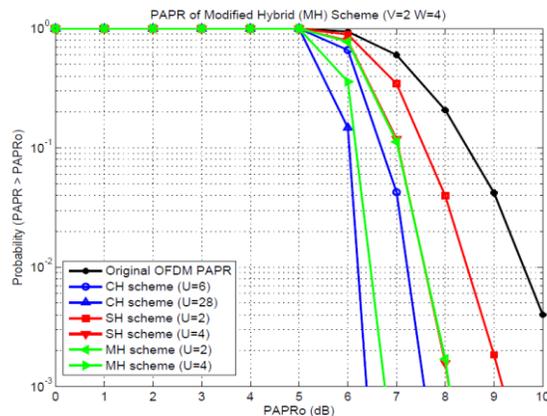


Figure 8: PAPR reduction performance of switching hybrid scheme for OFDM systems

VI. CONCLUSION

In general, the PAPR reduction performance becomes better as the number of U increases in CH scheme, but the CH scheme has high computational complexity because of the increase of the number of IFFT. Therefore, based on original signals of CH scheme, several powerful algorithms have been proposed to improve high PAPR reduction performance without increasing the number of IFFT, including AH, SH and MH schemes. The MH scheme can obtain the best PAPR reduction performance by combining the AH with SH schemes. After a number of comparative simulations, the MH scheme has shown that the excellent PAPR reduction performance can be achieved without increasing the number of IFFT. The proposed MH scheme has obtained a superior PAPR reduction performance for OFDM systems. The technique has a better PAPR reduction performance by increasing the number of alternative OFDM sequences. In particular, when the number of IFFT is the same, the MH scheme has the best PAPR reduction compared with CH, AH and SH schemes. Therefore, for the MH scheme, it can expend less IFFT units to obtain similar PAPR reduction performance without the dramatic increase of side information bits.

REFERENCES

- [1] Rahmatallah, Y. and Mohan, S, "Peak-To-Average Power Ratio Reduction in OFDM Systems: A Survey and Taxonomy," IEEE Communications Surveys & Tutorials, vol. 15, No. 4, pp. 1567-1592, Fourth quarter 2013.
- [2] S.-H. Han and J.-H. Lee, "An Overview of Peak-to-Average Power Ratio Reduction Techniques for Multicarrier Transmission," IEEE Transactions on Wireless Communications, Vol. 12, No. 2, pp. 56-65, Apr. 2005.
- [3] P. A. Pushkarev, K.-W. Ryu, K.-Y. Yoo and Y.-W. Park, "A Study on the PAR Reduction by Hybrid Algorithm Based on the PTS and SLM Techniques," Proceedings of the 57th IEEE Vehicular Technology Conference, Vol. 2, pp. 1263-1267, 2003.
- [4] S.-J. Heo, H.-S. Noh, J.-S. No and D.-J. Shin, "A Modified SLM Scheme with Low Complexity for PAPR Reduction of OFDM Systems," IEEE Transactions on Broadcasting, Vol. 53, No. 4, pp. 804-808, Dec. 2007.
- [5] Komal Gupta, Monika Kushwaha, AbhayPratap Sharma &Arvind Singh Panwar et.al, "PAPR Reduction of OFDM Using a New Phase Sequence in SLM Technique" International Journal of Advanced Electrical and Electronics Engineering (IJAEED), ISSN (Print) : 2278- 8948, Volume-2, Issue-2, 2013.
- [6] Poonam Kundu, Prabhjot Kauret.al, "Comparison of Peak to Average Power Reduction Techniques in OFDM" 978-1-4799-3080-7/14 c_2014 IEEE.
- [7] Tao Jiang and Yiyan Wu, "PAPR reduction of OFDM signals using Partial Transmit Sequence with Low Computational Complexity," IEEE Transactions on Broadcasting, vol. 53, no. 3, pp. 719-724, September 2007.
- [8] Jung Chien Chen, "Partial Transmit Sequences for Peak to Average Power Ratio Reduction of OFDM Signals with the Cross Entropy Method," IEEE signal processing Letters, vol. 16, no.6, pp.545-548, June 2009.
- [9] Sheng. Ju. Ku, Chin. Liang. Wang and Chiuan. Hsu. Chen, "A reduced-complexity PTS-based PAPR reduction scheme for OFDM systems," IEEE Trans. Wireless Communication, vol. 9, no. 8, pp. 2455-2460, Aug. 2010.
- [10] Yajun Wang, Wen Chen, and ChinthaTellambura "A PAPR Reduction Method Based on Artificial Bee Colony Algorithm for OFDM Signals", IEEE Transactions on Wireless Communications, vol. 9, no. 10, pp. 2994-2999, October 2010.
- [11] Jung Chien Chen, "Application of Quantum Inspired Evolutionary Algorithm to Reduce PAPR of an OFDM Signal Using Partial Transmit Sequence Technique," IEEE Transactions on Broadcasting, vol. 56, no. 1, pp. 110-113, March 2010.
- [12] J. Hou, J. Ge and J. Li, "Peak-to-average power ratio reduction of OFDM signals using PTS scheme with low computational complexity," IEEE Trans. Broadcast., vol. 57, no. 1, pp. 143-148, Mar. 2011.
- [13] Lingyin Wang and Ju Liu, "PAPR Reduction of OFDM Signals by PTS With Grouping and Recursive Phase Weighting Methods," IEEE Transactions on Broadcasting, vol.57, no.2, pp.299-306, June 2011.
- [14] Miin-Jong Hao and Chiu Hsiung Lai., "Precoding for PAPR Reduction of OFDM Signals With Minimum Error Probability," IEEE Transactions on Broadcasting, vol. 56, no. 1, pp. 120-128, November 2010.
- [15] H.D. Joshi and R. Saxena, "OFDM and its Major Concerns: A Study with Way Out," IETE Journal of Education, vol. 54, Issued. 1, pp. 1-49, Jan-Jun. 2013.